

$$\mathrm{rank}(J) \equiv \dim_{\mathbb{C}}(x_1, \dots, x_n) R_n/J \equiv m$$